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REVIEW PROBLEMS FOR INTERMEDIATE ALGEBRA ASSESSMENT TEST-Rev 1

- 1. Simplify and combine like terms: -18x + 3(2x 8) 9x (4 6x)
- 2. Multiply: $(2z^3 4z^2 + 6z 1)(3z + 2)$
- 3. Multiply: $(2a + 3)(4a^2 6a + 9)$
- 4. Multiply: (5x 2)(3x + 4)

5.
$$3\sqrt{25} = 6^2 v^3 z^5$$

6.
$$\frac{6y^2}{6^4y^2z^7} =$$

7.
$$\frac{5^0 (x^2)^3 y}{5x (y^2)^5} =$$

8.
$$\frac{7a^{3}(b+c)^{2}}{14a(b+c)} =$$

9.
$$3^{2^4} =$$

10. $16^{\frac{5}{4}} =$

11. Simplify. All exponents must be positive.

$$\left(\frac{x^{-\frac{3}{5}}z^{-1}}{2^{-2}z^{-\frac{1}{2}}x}\right)^{-1} =$$

- 12. Solve: 7z 3z + 12 5 = 8z + 7
- 13. Solve: -4(3 + 2m) m = -3m
- 14. Solve for x: Q = 3x + 2y + 4z
- 15. Solve for x: $4^x = 8^{x-3}$
- 16. Scott Hardy invested some money at 12% and \$4000 less than this amount at 14%. Find the amount invested at each rate if his total annual interest income is \$4,120.
- 17. A pharmacist needs 100 liters of a 50% alcohol solution. She has a 30% alcohol solution and an 80% alcohol solution that she can mix. How many liters of each does she need?
- 18. Two people need to sort a pile of bottles at the recycling center. Working alone, one person could do the entire job in 9 hours, and the other person could do the entire job in 6 hours. How long would it take them to complete the job if they work together?

- 19. Solve the system: 2x + 3y = 10-3x + 2y = 11
- 20. Solve the system: 3x + 4y = 86x = 7 - 8y
- 21. Steve and Ross must paint Steve's entire house. Steve bought 3 gallons of paint and 2 brushes at one store for \$48. Ross bought 5 gallons of paint and 1 brush at another store for \$66. Assuming the price per gallon and cost per brush were the same at both stores, find what they paid per gallon for paint and the cost per brush.
- 22. Solve: $\frac{2q+1}{3} \frac{q-1}{4} = -2$

23. Solve:
$$5x^2 - 3x = 0$$

- 24. Find the roots of the following equation by factoring: $10x^2 13x = 3$
- 25. Find the roots of the following equation using the quadratic formula:

$$2x^2 + 3x = 10$$

- 26. Find the roots of the following equation: (2x + 1)(x 2) = -3
- 27. Solve: $\frac{y}{3} \frac{y}{7} = 1$ 28. Solve: $\frac{1}{m+4} - \frac{3}{2m+8} = \frac{1}{2}$
- 29. Rationalize the denominator and simplify: $\frac{-6\sqrt{3}}{\sqrt{2}}$
- 30. Multiply and combine like terms: $(2x + 3)^2$
- 31. Multiply and combine like terms: $(2x + 3)^2 (x + 2)^2$
- 32. Evaluate the following expression if x = 3 and y = -2.

$$3x^2y-4xy^2\\$$

33. Find the distance between the point (-4, -2) and the point (6, -1).

34. Divide:
$$\frac{8m^4 - 6m^3 + 2m}{2m}$$

35. Divide:
$$(15p^2 + 11p - 17) \div (3p - 2)$$

36. What quadrant is the point (-3,10) in?

37. Reduce, if possible:
$$\frac{6x^2 + 7x - 5}{3x + 5}$$

38. Multiply:
$$\frac{2p^2 - 5p - 12}{5p^2 - 18p - 8} \cdot \frac{25p^2 - 4}{30p - 12}$$

39. Divide:
$$\frac{25p^3q^2}{8p^4q} \div \frac{15pq^2}{16p^5}$$

40. Divide:
$$(y^2 + 2y) \div \frac{y+5}{y^2+4y-5}$$

41. Combine:
$$\frac{3}{t-2} - \frac{5}{2-t}$$

42. Combine:
$$\frac{2}{y+1} + \frac{6}{y-1}$$

43. Combine:
$$\frac{3r}{10r^2 - 3rs - s^2} + \frac{2r}{2r^2 + rs - s^2}$$

44. Simplify:
$$\frac{\frac{3}{x}-5}{6+\frac{1}{x}}$$

45. Sketch the graph of the line 3x - y = 4.

- 46. If the slope, m, of line is $\frac{1}{2}$, and the y- intercept is at (0, 3), what is the equation of the line? Express the answer in slope-intercept form.
- 47. What is the slope of the line between the two points (4, -3) and (-2, -1)?
- 48. What is the equation of the line with slope = $\frac{2}{3}$ and containing point (2, -1)? Express the answer in standard form.
- 49. What is the equation of the line which goes through the two points (3, 5) and (-1, 0)? Express the answer in standard form.
- 50. Sketch the graph of the line y = -2.
- 51. Solve $\sqrt{x+2} = x-4$
- 52. Solve |x 2| < 3
- 53. 4! =
- 54. Solve -3x > 12 + x

- 5 - SOLUTIONS FOR INTERMEDIATE ALGEBRA ASSESSMENT TEST

1. -18x + 3(2x - 8) - 9x - (4 - 6x)

Use the distributive law to remove parentheses:

-18x + 6x - 24 - 9x - 4 + 6x

Combine like terms: -15x - 28

2. Multiply vertically to easily line up like terms:

$$2z^{3} - 4z^{2} + 6z - 1$$

$$3z + 2$$

$$6z^{4} - 12z^{3} + 18z^{2} - 3z$$

$$4z^{3} - 8z^{2} + 12z - 2$$

$$6z^{4} - 8z^{3} + 10z^{2} + 9z - 2$$

3. Multiply vertically as in #2.

answer:
$$8a^3 + 27$$

4. Multiply using the acronym FOIL (firsts, outsides, insides, lasts) $(5x-2)(3x+4) = 15x^2 + 20x - 6x - 8$ $= 15x^2 + 14x - 8$

5. $3^{\sqrt{25}} = 3^5 = 3 \cdot 3 \cdot 3 \cdot 3 \cdot 3 = 243$

6. When dividing, the base stays the same and you subtract exponents negative exponents then go to the denominator:

$$\frac{6^2 y^3 z^5}{6^4 y^2 z^7} = \frac{y}{6^2 z^2} = \frac{y}{36z^2}$$

7. When raising a power to a power, you multiply exponents. Any non-zero expression raised to the zero power is 1.

$$\frac{5^{0}(x^{2})^{3}y}{5x(y^{2})^{5}} = \frac{1x^{6}y}{5xy^{10}} = \frac{x^{5}}{5y^{9}}$$
8. $\frac{7a^{3}(b+c)^{2}}{14a(b+c)} = \frac{a^{2}(b+c)}{2}$
 $\frac{(b+c)^{2}}{b+c}$ works exactly like $\frac{x^{2}}{x}$. Just as $\frac{x^{2}}{x} = x$, $\frac{(b+c)^{2}}{b+c} = (b+c)^{1}$ or $(b+c)$
9. $3^{2^{4}} = 3^{16}$

10. $16^{\frac{5}{4}}$ means the 4th root of 16 to the 5th power:

$$(\sqrt[4]{16})^5 = 2^5 = 32$$

11. Remember, to raise a power to a power, multiply exponents.

$$\left(\frac{x^{-\frac{3}{5}}z^{-1}}{2^{-2}z^{-\frac{1}{2}}x}\right)^{-1} = \frac{x^{\frac{3}{5}}z^{1}}{2^{2}z^{\frac{1}{2}}x^{-1}}$$

The x^{-1} must go to the numerator and become x^{1} :

$$\frac{x^{\frac{3}{5}}x^{1}z^{1}}{4z^{\frac{1}{2}}}$$

When multiplying, add exponents. When dividing, subtract exponents.

$$\frac{=x^{\frac{8}{5}}z^{\frac{1}{2}}}{4}$$

12. 7z - 3z + 12 - 5 = 8z + 7

Combine like terms:

4z + 7 = 8z + 7Add -4z to both sides: 7 = 4z + 7Add -7 to both sides: 0 = 4zDivide both sides by 4: 0 = z 13. -4(3+2m) - m = -3m

Use the distributive law to remove parentheses:

-12 - 8m - m = -3m-12 - 9m = -3m

Add 9m to both sides: -12 = 6mDivide both sides by 6: -2 = m

14.
$$Q = 3x + 2y + 4z$$

Add -2y - 4z to both sides in order to isolate the term containing the unknown, x:

Q - 2y - 4z = 3x

Divide both sides by 3: $\frac{Q-2y-4z}{3} = x$

15. $4^{x} = 8^{x-3}$

Rewrite 4 and 8 as powers of 2: $(2^2)^x = (2^3)^{x-3}$ When raising a power to a power, you multiply exponents: $2^{2x} = 2^{3x-9}$ Hence, 2x = 3x - 9-x = -9x = 9

16. Let x = the amount of money invested at 12%.

x - 4000 = the amount of money invested at 14%.

Then, .12x + .14(x - 4000) = 4120

Multiply each term by 100 to remove decimal points:

12x + 14(x - 4000) = 412,000 12x + 14x - 56000 = 412,000 26x = 468,000 x = 18,000He invested \$18,000 at 12% and \$14,000 at 14% - 8 -

17. Let x = amount of 30% alcohol solution. y = amount of 80% alcohol solution.

Equate amount of solution: x + y = 100

Equate amount of alcohol: .30x + .80y = .50(100)or 30x + 80y = 50(100)

If x + y = 100, then y = 100 - x

$$30x + 80(100 - x) = 5000$$

$$30x + 8000 - 80x = 5000$$

$$-50x = -3000$$

$$x = 60$$

She needs 60 liters of the 30% solution and 40 liters of the 80% solution.

 First person takes 9 hours. Second person takes 6 hours. Together they take x hours.

Equate what can be done in 1 hour.

$$\frac{1}{9} + \frac{1}{6} = \frac{1}{x}$$

Multiply both sides by the L. C. D = 18x:

$$2x + 3x = 18$$

$$5x = 18$$

$$x = \frac{18}{5} \text{ or } 3\frac{3}{5}$$

Together it would take $3\frac{3}{5}$ hours.

19.
$$2x + 3y = 10$$

 $-3x + 2y = 11$

Multiply the top equation by 3 and the bottom by 2 so that the x terms will be eliminated.

$\frac{-6x + 4y = 22}{13y = 52}$ 2x 2x 2x	bstitute $y = 4$ in the first equation: + $3(4) = 10$ + $12 = 10$ = -2 = -1
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20. 3x + 4y = 86x = 7 - 8y

In the second equation add 8y to both sides to get it in standard form:

$$3x + 4y = 8$$
$$6x + 8y = 7$$

Multiply the top equation by -2:

$$-6x - 8y = -16$$
$$6x + 8y = 7$$
$$0 = -9$$

That cannot happen. The lines are parallel and the system is inconsistent.

21. Let g = price for one gallon of paint Let b = price for one brush

> 3g + 2b = 485g + b = 66

In the second equation: b = 66 - 5g. Substitute this into the top equation:

$$3g + 2(66 - 5g) = 48$$

$$3g + 132 - 10g = 48$$

$$-7g + 132 = 48$$

$$-7g = -84$$

$$g = 12$$

b = 66 - 5g = 66 - 5(12) = 66 - 60 = 6

A gallon of pain costs \$12; one brush costs \$6.

22.
$$\frac{2q+1}{3} - \frac{q-1}{4} = -2$$

Multiply both sides by 12 to eliminate the denominators:

$$4(2q + 1) - 3(q - 1) = -2(12)$$

$$8q + 4 - 3q + 3 = -24$$

$$5q + 7 = -24$$

$$5q = -31$$

$$q = -\frac{31}{5}$$

- 10 -

23. $5x^2 - 3x = 0$

Factor out the common factor of x: x(5x - 3) = 0

The product of two factors is 0, and hence one of the factors is 0: x = 0 or 5x - 3 = 05x = 3

$$x = \frac{3}{5}$$

24. $10x^2 - 13x = 3$

Add -3 to both sides so that 0 is on one side of the equation:

 $10x^2 - 13x - 3 = 0$

Factor the left hand side:

(5x + 1 = 0)(2x - 3) = 0

The product of two factors is 0, and hence one of the factors is 0:

$$5x + 1 = 0 \text{ or } 2x - 3 = 0$$

$$5x = -1 \qquad 2x = 3$$

$$x = -\frac{1}{5} \qquad x = \frac{3}{2}$$

25.
$$2x^2 + 3x = 10$$

Add -10 to both sides so that 0 is on one side of the equation:

$$2x^2 + 3x - 10 = 0$$

The quadratic formula says that in the quadratic equation $ax^2 + bx + c = 0$,

$$\mathbf{x} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

In the given equation, then, a = 2, b = 3, and c = -10

$$x = \frac{-3 \pm \sqrt{3^2 - 4(2)(-10)}}{2(2)} = \frac{-3 \pm \sqrt{9 + 80}}{4} = \frac{-3 \pm \sqrt{89}}{4}$$

26. (2x+1)(x-2) = -3

First multiply the 2 binomials: $2x^2 - 3x - 2 = -3$

Add 3 to both sides: $2x^2 - 3x + 1 = 0$

Factor: (2x - 1)(x - 1) = 0

2x - 1 = 0 or x - 1 = 0 $2x = 1 \qquad x = 1$ $x = \frac{1}{2}$

27.
$$\frac{y}{3} - \frac{y}{7} = 1$$

Multiply both sides by 21:
$$7y - 3y = 21$$
$$4 y = 21$$
$$y = \frac{21}{4}$$

28.
$$\frac{1}{m+4} - \frac{3}{2m+8} = -\frac{1}{2}$$

Factor the denominators, wherever possible:

$$\frac{1}{m+4} - \frac{3}{2(m+4)} = -\frac{1}{2}$$

Multiply both sides by the L. C. D. of 2(m + 4):

$$1(2) - 3 = -1(m + 4)$$

 $2 - 3 = -m - 4$
 $3 = -m$
 $-3 = m$

29.

$$\frac{-6\sqrt{3}}{\sqrt{2}}$$

Multiply numerator and denominator by $\sqrt{2}$:

$$\frac{-6\sqrt{3}}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{-6\sqrt{6}}{2} = -3\sqrt{6}$$

30.
$$(2x+3)^2 = (2x+3)(2x+3) = 4x^2 + 6x + 6x + 9$$

= $4x^2 + 12x + 9$

31.
$$(2x + 3)^2 - (x + 2)^2$$

From problem #30 $(2x + 3)^2 = 4x^2 + 12x + 9$

Then,
$$(x + 2)^2 = (x + 2)(x + 2) = x^2 + 2x + 2x + 4 = x^2 + 4x + 4$$

$$(2x + 3)^{2} - (x + 2)^{2} = 4x^{2} + 12x + 9 - (x^{2} + 4x + 4)$$

= 4x² + 12x + 9 - x² - 4x - 4
= 3x² + 8x + 5

32. $3x^2y - 4xy^2$

If x = 3 and y = -2, then the problem becomes:

$$3(3)^{2}(-2) - 4(3)(-2)^{2} = 3(9)(-2) - 4(3)(4) = -54 - 48 = -102$$

33. The distance between points (x_1, y_1) and (x_2, y_2) is given by the formula:

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

The given points are (-4, -2) and (6, -1)
 $x_1 = -4;$ $x_2 = 6$
 $y_1 = -2;$ $y_2 = -1$
Notice that $x_2 - x_1 = 6 - (-4) = 6 + 4 = 10$
 $y_2 - y_1 = -1 - (-2) = -1 + 2 = 1$

Therefore, $d = \sqrt{10^2 + 1^2} = \sqrt{100 + 1} = \sqrt{101}$

34.
$$\frac{8m^4 - 6m^3 + 2m}{2m} = \frac{8m^4}{2m} - \frac{6m^3}{2m} + \frac{2m}{2m} = 4m^3 - 3m^2 + 1$$

35.
$$3p-2\frac{5p+7+\frac{-3}{3p-2}}{15p^2+11p-17}$$

 $15p^2-10p$
 $21p-17$
 $21p-14$
 -3

36. Quadrant II

37.
$$\frac{6x^2 + 7x - 5}{3x + 5} = \frac{(3x + 5)(2x - 1)}{3x + 5} = 2x - 1$$

38.
$$\frac{2p^2 - 5p - 12}{5p^2 - 18p - 8} \cdot \frac{25p^2 - 4}{30p - 12} = \frac{(2p + 3)(p - 4)}{(5p + 2)(p - 4)} \cdot \frac{(5p - 2)(5p + 2)}{6(5p - 2)} = \frac{2p + 3}{6}$$

$$39. \qquad \frac{25p^3q^2}{8p^4q} \div \frac{15pq^2}{16p^5}$$

To divide fraction, invert the divisor and multiply:

$$\frac{5 p^2 2}{25p^3q^2} \cdot \frac{2 p}{15pq^2} = \frac{10p^3}{3q}$$

40. To divide fractions, invert the divisor and multiply:

$$(y^{2} + 2y) \div \frac{y+5}{y^{2} + 4y - 5} = (y^{2} + 2y) \cdot \frac{y^{2} + 4y - 5}{y+5}$$
$$= y(y+2) \cdot \frac{(y+5)(y-1)}{y+5} = y(y+2)(y-1)$$

41. $\frac{3}{t-2} - \frac{5}{2-t}$ Note that 2 - t = (-1)(t - 2). The problem can then be written: $\frac{3}{t-2} - \frac{5}{(-1)(t-2)}$

The two negatives become positive: = $\frac{3}{t-2} + \frac{5}{t-2} = \frac{8}{t-2}$

42.
$$\frac{2}{y+1} + \frac{6}{y-1}$$

The L. C. D. is
$$(y + 1)(y - 1)$$
: $\frac{2(y - 1)}{(y + 1)(y - 1)} + \frac{6(y + 1)}{(y + 1)(y - 1)}$

$$=\frac{2y-2+6y+6}{(y+1)(y-1)}=\frac{8y+4}{(y+1)(y-1)}or\frac{4(2y+1)}{(y+1)(y-1)}$$

43.
$$\frac{3r}{10r^2 - 3rs - s^2} + \frac{2r}{2r^2 + rs - s^2}$$

Factor the denominators:

$$\frac{3r}{(5r+s)(2r-s)} + \frac{2r}{(2r-s)(r+s)}$$

The L. C. D. is
$$(5r + s)(2r - s)(r + s)$$

$$\frac{3r(r + s)}{(5r + s)(2r - s)(r + s)} + \frac{2r(5r + s)}{(2r - s)(r + s)(5r + s)}$$

$$= \frac{3r^2 + 3rs + 10r^2 + 2rs}{(5r + s)(2r - s)(r + s)} = \frac{13r^2 + 5rs}{(5r + s)(2r - s)(r + s)}$$

$$44. \qquad \frac{\frac{3}{x}-5}{6+\frac{1}{x}}$$

In the numerator, the L. C. D. is x and it becomes:

$$\frac{3-5x}{x}$$

Similarly, the denominator is:

6x + 1x

Invert the denominator, and multiply:

 $\frac{3-5x}{x} \bullet \frac{x}{6x+1} = \frac{3-5x}{6x+1}$

3x - y = 445.

One way to sketch this is to plot 3 points and then connect the points.

1) If x = 0, then y = -4. 2) If x = 1, then y = -1. 3) If x = 2, then y = 2.

46. Slope-intercept form is y = mx + b where m is the slope and b is the y-intercept. This problem states that the slope is $\frac{1}{2}$ and the y-intercept in at (0, 3). Hence, the equation is:

$$y = \frac{1}{2}x + 3$$

Slope is defined to be: $m = \frac{change}{change} \frac{in}{in} \frac{y}{x} = \frac{y_2 - y_1}{x_2 - x_1}$ Given the point (4, -3) and (-2, -1): $m = \frac{-3 - (-1)}{4 - (-2)} = \frac{-3 + 1}{4 + 2} = \frac{-2}{6} = \frac{-1}{3}$

47.

- 48. The point-slope form of an equation is: $m(x - x_1) = y - y_1$ Given $m = \frac{2}{3}$ and the point = (2, -1), the equation is: $\frac{2}{3}(x - 2) = y - (-1)$ $\frac{2}{3}x - \frac{4}{3} = y + 1$ Multiply by 3: 2x - 4 = 3y + 3 2x - 3y = 7
- 49. Pts: (3, 5) and (-1, 0) = The slope, m, $=\frac{5-0}{3-(-1)}=\frac{5}{3+1}=\frac{5}{4}$ Using point (-1, 0) and the point-slope form from problem 48: $\frac{5}{4}(x+1) = y - 0$ $\frac{5}{4}x + \frac{5}{4} = y$ 5x + 5 = 4y5x - 4y = -5
- 50. Since y is always equal to -2, the graph is a horizontal line 2 units below the x-axis.

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51. Solve $\sqrt{x+2} = x-4$ Since a square root is involved, square both sides:

 $(\sqrt{x+2})^2 = (x-4)^2$ Then you get $x + 2 = x^2 - 8x + 16$. Set = 0 getting $x^2 - 9x + 14 = 0$. Factor the quadratic getting (x-7)(x-2) = 0. Solving you get x = 7 or x = 2. 7 checks but 2 does not, so the answer is x = 7.

- 52. Solve |x-2| < 3 For absolute value with less than, there are two cases: x-2 < 3 and x-2 > -3. Solving the first gives x < 5; solving the second gives x > -1. Therefore -1 < x < 5
- 53. $4! = 4 \ge 3 \ge 2 \ge 1 = 24$
- 54. -3x > 12 + x Subtract x from both sides gives -4x > 12. Divide both sides by -4 giving x < -3. Remember, when you multiply or divide an inequality by a negative, the inequality reverses.